

“90 subjects diagnosed for depression enlisted for comparison of treatments for depression. Subjects were randomly divided into three groups 30 ea and given pills to take over 3 months.”
 Desired to test H0: rate of return to depression same for all three types of pill vs H1: not all same.

STT 200 4-27-096

observed table H₀: RATE OF DEPR SAME FOR ALL 3 TREATMENTS

	Placebo	Saint John's wort	Posrex	
Depression returned	24 (OBS)	22	14	60
No sign of depression	6	8	16	30
fixed totals	30	30	30	90

TEST OF Homogeneity

$$\chi^2_{STAT} = \sum \frac{(OBS - EXP)^2}{EXP}$$

6 CELLS BUT DF (R-1)(C-1) = (2-1)(3-1) = 2

“expected” table under H0

	Placebo	Saint John's wort	Posrex	
Depression returned	20 (exp)	20	20	
No sign of depression	10	10	10	
fixed totals	30	30	30	90

WANT THIS BIG IF YOU ARE "POSREX"

Chi square statistic = $(24 - \frac{30 \cdot 60}{90})^2 / (\frac{30 \cdot 60}{90}) + \dots = 0.8 + 0.2 + 1.8 + 1.6 + 0.4 + 3.6 = 8.4$

with df = (R-1)(C-1) = (2-1)(3-1) = 2.

P-value = Pr(chi square with 2 df > 8.4) = 0.015. ← CALC 1.5% FAIRLY SMALL EVIDENCE AGAINST H₀ CELL OF INTEREST

0.025 ← P VALUE BETWEEN → 0.01

2 df 7.378 (8.4 is in between) 9.210 so P-value is between 0.025 and 0.01.



Binomial: p = probability of "success," $q = 1 - p$.

CH 19 -

17-21. IF more than 20% of emergency responders require additional training THEN additional money will have to be found.

17. Suggest H_0 and H_1 for a z-test to address the issue.

SAMPLE n RESPONDERS TO SEE IF THERE IS EVIDENCE
 $p > .2$ ($p = P_p^N$ FRACTION NEEDING TRAINING).

COULD TEST $H_0: p = p_0 = .2$ vs $H_1: p > .2$

ALL TESTS STAY ON H_0 UNLESS LOTS OF EVIDENCE TO CONTRARY.

SHIPPER WANTS

$H_0: p \leq .2$

$H_1: p > .2$

RECEIVER

$H_0: p \geq .2$

$H_1: p < .2$

18. A random sample of 200 emergency responders finds 50 who require the training. Calculate an appropriate z-test statistic.

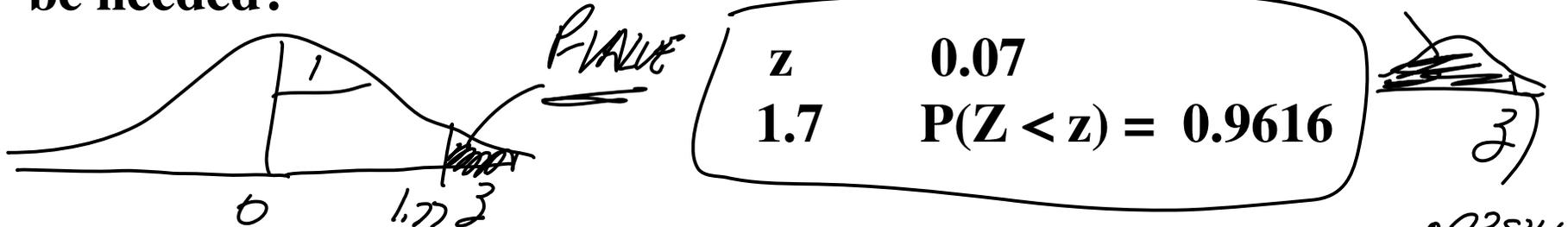
$H_0: p \leq .2$
 $H_1: p > .2$

$\hat{p} = \frac{50}{200} = .25$

$z\text{-TEST} = \frac{\hat{p} - p_0}{\sqrt{p_0(1-p_0)/n}} = \frac{.25 - .2}{\sqrt{.2 \cdot .8 / 200}} = 1.77$

$p_0 = 1 - p_0 = .8$
 $p_0 = .2$

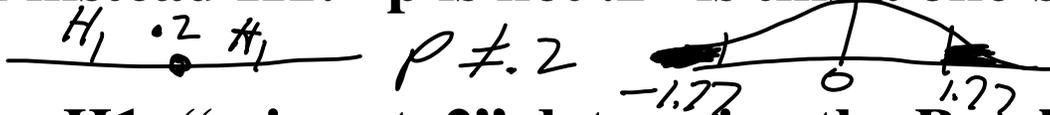
19. Determine the P-value. Does it seem that additional money will be needed?



ans. P-value $\sim P(Z > 1.77) = 1 - 0.9616 = 0.0384$.

(IF THIS IS ~ 0 REJECT H_0 (SO IF WISH $\alpha = .01$ THEN REJECT IF $.0384 < .01$ NO)

20. If instead H_1 : "p is not .2" is this a one-sided or two-sided test?



21. For H_1 : "p is not .2" determine the P-value from (19).

ans. $2(0.0384) = 0.0768$ TOO BIG FAIL TO REJECT H_0

TWICE \rightarrow P-VAL OF 1 SIDED (1 TAILED) TEST

22. For a test of $H_0: p = 0.2$ versus $H_1: "p \text{ is not } 0.2"$ we may employ chi square goodness of fit. Give the table of exp and obs counts for such a test if a sample of 200 finds 50 (as above).

$n=200$	exp	$.2(200) = 40$	160	GOODNESS OF FIT $C=2$ $DF=2-1=1$
	obs	50	150	

require training do not require training

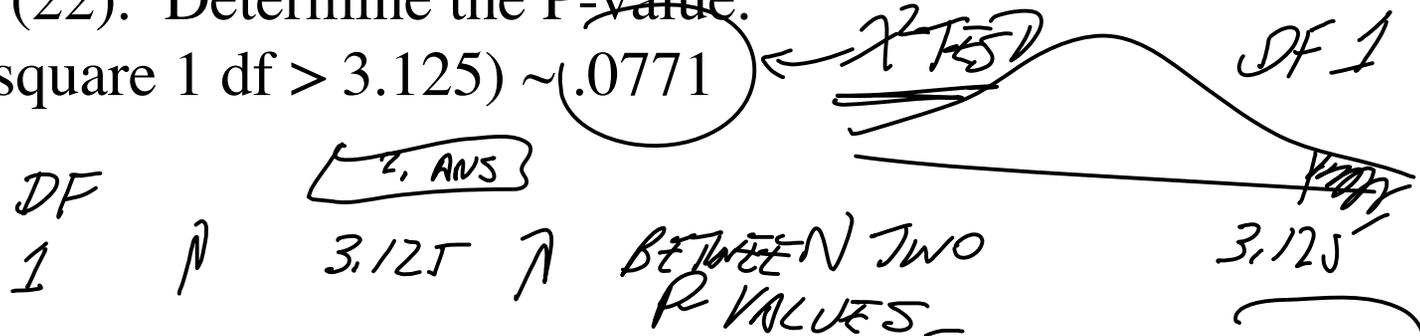
std score

23. Refer to (22). Determine the chi square statistic for the test.

$$\chi^2_{STAT} = \sum_{2 \text{ CELLS}} \frac{(OBS - exp)^2}{exp} = \frac{(50 - 40)^2}{40} + \frac{(150 - 160)^2}{160} = 3.125$$

24. Refer to (22). Determine the P-value.

$\Pr(\text{chi square } 1 \text{ df} > 3.125) \sim .0771$



Compare P-value with that of two-sided z-test (which was 0.0768).

Z -TEST \rightarrow BINOM p